## X100/301

NATIONAL
QUALIFICATIONS 2005

FRIDAY, 20 MAY
9.00 AM - 10.10 AM

MATHEMATICS<br>HIGHER<br>Units 1, 2 and 3<br>Paper 1<br>(Non-calculator)

## Read Carefully

1 Calculators may NOT be used in this paper.
2 Full credit will be given only where the solution contains appropriate working.
3 Answers obtained by readings from scale drawings will not receive any credit.

## ALL questions should be attempted.

1. Find the equation of the line ST, where T is the point $(-2,0)$ and angle STO is $60^{\circ}$.

2. Two congruent circles, with centres A and B, touch at P .

Relative to suitable axes, their equations are
$x^{2}+y^{2}+6 x+4 y-12=0$ and $x^{2}+y^{2}-6 x-12 y+20=0$.
(a) Find the coordinates of P .
(b) Find the length of AB .

3. D,OABC is a pyramid. A is the point $(12,0,0), B$ is $(12,6,0)$ and D is $(6,3,9)$.
$F$ divides DB in the ratio 2:1.
(a) Find the coordinates of the point F .
(b) Express $\overrightarrow{\mathrm{AF}}$ in component form.

4. Functions $f(x)=3 x-1$ and $g(x)=x^{2}+7$ are defined on the set of real numbers.
(a) Find $h(x)$ where $h(x)=g(f(x))$.
(b) (i) Write down the coordinates of the minimum turning point of $y=h(x)$.
(ii) Hence state the range of the function $h$.

2
6. (a) The terms of a sequence satisfy $u_{n+1}=k u_{n}+5$. Find the value of $k$ which produces a sequence with a limit of 4 .
(b) A sequence satisfies the recurrence relation $u_{n+1}=m u_{n}+5, u_{0}=3$.
(i) Express $u_{1}$ and $u_{2}$ in terms of $m$.
(ii) Given that $u_{2}=7$, find the value of $m$ which produces a sequence with no limit.
7. The function $f$ is of the form $f(x)=\log _{b}(x-a)$. The graph of $y=f(x)$ is shown in the diagram.
(a) Write down the values of $a$ and $b$.
(b) State the domain of $f$.

(a) Show that $(x-3)$ is a factor of $f(x)$, and hence factorise $f(x)$ fully.
(b) Find the coordinates of the points where the curve with equation $y=f(x)$ crosses the $x$ - and $y$-axes.
(c) Find the greatest and least values of $f$ in the interval $-2 \leq x \leq 2$.
9. If $\cos 2 x=\frac{7}{25}$ and $0<x<\frac{\pi}{2}$, find the exact values of $\cos x$ and $\sin x$.
10. (a) Express $\sin x-\sqrt{3} \cos x$ in the form $k \sin (x-a)$ where $k>0$ and $0 \leq a \leq 2 \pi$.

4
(b) Hence, or otherwise, sketch the curve with equation $y=3+\sin x-\sqrt{3} \cos x$ in the interval $0 \leq x \leq 2 \pi$.

5
11. (a) A circle has centre ( $t, 0$ ), $t>0$, and radius 2 units.
Write down the equation of the circle.
(b) Find the exact value of $t$ such that the line $y=2 x$ is a tangent to the circle.


## X100/303

| NATIONAL | FRIDAY, 20 MAY | MATHEMATICS |
| :--- | :--- | :--- |
| QUALIFICATIONS | $10.30 \mathrm{AM}-12.00$ NOON | HIGHER |
| 2005 |  | Units 1, 2 and 3 |
|  |  | Paper 2 |

## Read Carefully

## 1 Calculators may be used in this paper.

2 Full credit will be given only where the solution contains appropriate working.
3 Answers obtained by readings from scale drawings will not receive any credit.

## ALL questions should be attempted.

1. Find $\int \frac{4 x^{3}-1}{x^{2}} d x, x \neq 0$.
2. Triangles ACD and BCD are right-angled at D with angles $p$ and $q$ and lengths as shown in the diagram.
(a) Show that the exact value of $\sin (p+q)$ is $\frac{84}{85}$.
(b) Calculate the exact values of:
(i) $\cos (p+q)$;
(ii) $\tan (p+q)$.

3. (a) A chord joins the points $\mathrm{A}(1,0)$ and $\mathrm{B}(5,4)$ on the circle as shown in the diagram.
Show that the equation of the perpendicular bisector of chord AB is $x+y=5$.

(b) The point C is the centre of this circle. The tangent at the point $A$ on the circle has equation $x+3 y=1$.


Find the equation of the radius CA .
4
(c) (i) Determine the coordinates of the point C.
(ii) Find the equation of the circle.
4. The sketch shows the positions of Andrew(A), $\operatorname{Bob}(B)$ and $\operatorname{Tracy}(T)$ on three hill-tops.
Relative to a suitable origin, the coordinates (in hundreds of metres) of the three people are $\mathrm{A}(23,0,8)$, $\mathrm{B}(-12,0,9)$ and $\mathrm{T}(28,-15,7)$.
In the dark, Andrew and Bob locate Tracy using heat-seeking beams.

(a) Express the vectors TA and TB in component form.
(b) Calculate the angle between these two beams.
5. The curves with equations $y=x^{2}$ and $y=2 x^{2}-9$ intersect at K and L as shown.
Calculate the area enclosed between the curves.

6. The diagram shows the graph of $y=\frac{24}{\sqrt{x}}, x>0$.

Find the equation of the tangent at P , where $x=4$.

7. Solve the equation $\log _{4}(5-x)-\log _{4}(3-x)=2, x<3$.

## Marks

8. Two functions, $f$ and $g$, are defined by $f(x)=k \sin 2 x$ and $g(x)=\sin x$ where $k>1$.
The diagram shows the graphs of $y=f(x)$ and $y=g(x)$ intersecting at O, A, B, C and D.
Show that, at A and $\mathrm{C}, \cos x=\frac{1}{2 k}$.

(5)
9. The value $V$ (in $£$ million) of a cruise ship $t$ years after launch is given by the formula $V=252 e^{-0.06335 t}$.
(a) What was its value when launched?
(b) The owners decide to sell the ship once its value falls below $£ 20$ million. After how many years will it be sold?
10. Vectors $\boldsymbol{a}$ and $\boldsymbol{c}$ are represented by two sides of an equilateral triangle with sides of length 3 units, as shown in the diagram.
Vector $\boldsymbol{b}$ is 2 units long and $\boldsymbol{b}$ is perpendicular to both $\boldsymbol{a}$ and $\boldsymbol{c}$.


Evaluate the scalar product $\boldsymbol{a} .(\boldsymbol{a}+\boldsymbol{b}+\boldsymbol{c})$.
4
11. (a) Show that $x=-1$ is a solution of the cubic equation $x^{3}+p x^{2}+p x+1=0$.
(b) Hence find the range of values of $p$ for which all the roots of the cubic equation are real.

## 2005 Mathematics

## Higher

## Finalised Marking Instructions

These Marking Instructions have been prepared by Examination Teams for use by SQA Appointed Markers when marking External Course Assessments.

## Mathematics Higher

## Instructions to Markers

1. Marks must be assigned in accordance with these marking instructions. In principle, marks are awarded for what is correct, rather than marks deducted for what is wrong.
2. Award one mark for each 'bullet' point. Each error should be underlined in RED at the point in the working where it first occurs, and not at any subsequent stage of the working.
3. The working subsequent to an error must be followed through by the marker with possible full marks for the subsequent working, provided that the difficulty involved is approximately similar. Where, subsequent to an error, the working is eased, a deduction(s) of marks(s) should be made.

This may happen where a question is divided into parts. In fact, failure to even answer an earlier section does not preclude a candidate from assuming the result of that section and obtaining full marks for a later section.
4. Correct working should be ticked $(\checkmark)$. This is essential for later stages of the SQA procedures. Where working subsequent to an error(s) is correct and scores marks, it should be marked with a crossed tick ( $\boldsymbol{X}$ or $\boldsymbol{X} \checkmark$ ). In appropriate cases attention may be directed to work which is not quite correct (eg bad form) but which has not been penalised, by underlining with a dotted or wavy line.

Work which is correct but inadequate to score any marks should be corrected with a double cross tick (
5. - The total mark for each section of a question should be entered in red in the outer right hand margin, opposite the end of the working concerned.

- Only the mark should be written, not a fraction of the possible marks.
- These marks should correspond to those on the question paper and these instructions.

6. It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

Where a candidate has scored zero marks for any question attempted, " 0 " should be shown against the answer.
7. As indicated on the front of the question paper, full credit should only be given where the solution contains appropriate working. Accept answers arrived at by inspection or mentally where it is possible for the answer so to have been obtained. Situations where you may accept such working will normally be indicated in the marking instructions.
8. Do not penalise:

- working subsequent to a correct answer
- legitimate variations in numerical answers
- correct working in the "wrong" part of the question
- omission of units
- bad form

9. No piece of work should be scored through without careful checking - even where a fundamental misunderstanding is apparent early in the answer. Reference should always be made to the marking scheme - answers which are widely off-beam are unlikely to include anything of relevance but in the vast majority of cases candidates still have the opportunity of gaining the odd mark or two provided it satisfies the criteria for the mark(s).
10. If in doubt between two marks, give an intermediate mark, but without fractions. When in doubt between consecutive numbers, give the higher mark.
11. In cases of difficulty covered neither in detail nor in principle in the Instructions, attention may be directed to the assessment of particular answers by making a referral to the PA. Please see the general instructions for PA referrals.
12. No marks should be deducted at this stange for careless or badly arranged work. In cases where the writing or arrangement is very bad, a note may be made on the upper left-hand corner of the front cover of the script.
13. Transcription errors: In general, as a consequence of a transcription error, candidates lose the opportunity of gaining either the first ic mark or the first pd mark.
14. Casual errors: In general, as a consequence of a casual error, candidates lose the opportunity of gaining either the first ic mark or the first pd mark.
15. Do not write any comments on the scripts. A revised summary of acceptable notation is given on page 4 .

## Summary

Throughout the examination procedures many scripts are remarked. It is essential that markers follow common procedures:

1. Tick correct working.
2. Put a mark in the right-hand margin to match the marks allocations on the question paper.
3. Do not write marks as fractions.
4. Put each mark at the end of the candidate's response to the question.
5. Follow through errors to see if candidates can score marks subsequent to the error.
6. Do not write any comments on the scripts.

## Remember - No comments on the scripts. Please use the following and nothing else.

_ $\boldsymbol{x} \quad$ The cross and underline. Underline an error and place a cross at the end of the line.
$X \quad$ The tick-cross. Use this to show correct or $\boldsymbol{X} \boldsymbol{\checkmark} \quad$ work where you are following through subsequent to an error.

The roof. Use this to show something is missing such as a crucial step in a proof of a 'condition' etc.


The tilde. Use this to indicate a minor transgression which is not being penalised (such as bad form).
*
The double-cross tick. Use this to show correct work but which is inadequate to score any marks. This may happen when working has been eased.

Bullets showing where marks have been allotted may be shown on scripts


Remember - No comments on the scripts. No abbreviations. No new signs.
Please use the above and nothing else.
All of these are to help us be more consistent and accurate.
Note: There is no such thing as a transcription error, a trivial error, a casual error or an insignificant error. These are all mistakes and as a consequence a mark is lost.

1 Find the equation of the line ST , where T is the point $(-2,0)$ and angle STO is $60^{\circ}$.


| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  | 3 | C | G2, G3 | NC | $05 / 6$ |

The primary method $\mathrm{m} / \mathrm{s}$ is based on the following generic $\mathrm{m} / \mathrm{s}$. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME

- ${ }^{1}$ SS use $m=\tan \theta$
- ${ }^{2}$ pd use exact value
- ${ }^{3}$ ic interpret result


## Notes

1 A candidate who states $m=\tan \left(\theta^{\circ}\right)$, and does not go on to use it earns no marks.

## Incompletion 1

$$
\begin{aligned}
& m=\tan \left(60^{\circ}\right) \\
& y-0=\tan \left(60^{\circ}\right)(x-(-2)) \\
& \bullet^{1} \quad \times \sqrt{ } \\
& \bullet^{2} \times \\
& \bullet^{3} \times \sqrt{ } \\
& \text { award } 2 \text { marks }
\end{aligned}
$$

## Common Error 1

$$
\begin{aligned}
& m=\sin \left(60^{\circ}\right) \\
& y-0=\frac{\sqrt{3}}{2}(x-(-2)) \\
& \bullet \quad \times \\
& \bullet^{2} \times \sqrt{ } \\
& \bullet^{3} \quad \times \sqrt{ }
\end{aligned}
$$

award 2 marks

Primary Method : Give 1 mark for each •

$$
\begin{array}{lll}
\bullet^{1} & m=\tan \left(60^{\circ}\right) & \text { stated or implied by } \bullet^{2} \\
\bullet^{2} & m=\sqrt{3} \\
\bullet^{3} & y-0=\sqrt{3}(x-(-2)) &
\end{array}
$$

## Alternative Method 1

- $1 \quad \mathrm{OS}=2 \tan \left(60^{\circ}\right)=2 \sqrt{3}$
-2 $m=\frac{2 \sqrt{3}}{2}=\sqrt{3}$
(cf $y=m x+c$ )
- ${ }^{3} y=\sqrt{3} x+2 \sqrt{3}$


## Alternative Method 2

- $\cos \left(60^{\circ}\right)=\frac{2}{S T}$ leading to

$$
S T=4 \text { and } O S=\sqrt{12}
$$

-2 $m=\frac{\sqrt{12}}{2}$
-3 $y-0=\frac{\sqrt{12}}{2}(x-(-2))$

2 Two congruent circles, with centres A and B , touch at P . Relative to suitable axes, their equations are $x^{2}+y^{2}+6 x+4 y-12=0$ and $x^{2}+y^{2}-6 x-12 y+20=0$.
(a) Find the coordinates of P .
(b) Find the length of AB.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | a | 3 | C | G9, G6 | CN | $05 / 18$ |
|  | b | 2 | C | G9 | CN |  |

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- ${ }^{1}$ ic interpret equ. of circle
- ${ }^{2}$ ic interpret equ. of circle
- ${ }^{3}$ pd process midpoint
- ${ }^{4}$ ss know how to find length
- 5 pd process


## Notes

1 at $\cdot 1, \cdot 2$
Each of the following may be awarded 1 mark from the first two marks
$A=(6,4)$ and $B=(-6,-12)$
$A=(-6,-4)$ and $B=(6,12)$
$A=(3,2)$ and $B=(-3,-6)$

2 At $\cdot 5$ stage, some errors lead to unsimplified surds. DO NOT accept unsimplified square roots of perfect squares (up to 100).
e.g. $\sqrt{ } 100$ would not gain $\cdot 5$.

Primary Method : Give 1 mark for each •
$\bullet{ }^{1}$
centre $\mathrm{A}=(-3,-2)$
centre $\mathrm{B}=(3,6)$
-3 $\quad \mathrm{P}=(0,2)$

- $\mathrm{AB}^{2}=(3-(-3))^{2}+(6-(-2))^{2} \quad$ [CE 1]
- ${ }^{5} \mathrm{AB}=10 \quad$ [Note 2]

2 marks

Alternative Method 1 for marks 1,2,3


Notes
1 Treat $\mathrm{P}=\begin{aligned} & 0 \\ & 2\end{aligned}$ as bad form.

## Alternative Method 2 for marks 4,5

- $r^{2}=3^{2}+2^{2}-(-12)$

$$
\text { or } r^{2}=(-3)^{2}+(-6)^{2}-20
$$

- ${ }^{5} \mathrm{AB}=2 r=10$

Alternative Method 3 for marks 4,5

$$
\begin{aligned}
\bullet & \overrightarrow{A B}=\begin{array}{l}
6 \\
8
\end{array} \\
\bullet & \mathrm{AB}=10
\end{aligned}
$$

$3 \mathrm{D}, \mathrm{OABC}$ is a pyramid. A is the point (12, 0,
$0), \mathrm{B}$ is $(12,6,0)$ and D is $(6,3,9)$.
F divides DB in the ratio 2:1.
(a) Find the coordinates of the point F.
(b) Express $A F$ in component form.


| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | a | 4 | C | G25 | CN | $05 / 24$ |
|  | b | 1 | C | G17 | CN |  |

The primary method $\mathrm{m} / \mathrm{s}$ is based on the following generic $\mathrm{m} / \mathrm{s}$. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME

- ${ }^{1}$ SS know to find DB
- ${ }^{2}$ ic interpret ratio
- ${ }^{3}$ pd process scalar times vector
- ${ }^{4}$ ic interpret vector and end points
- ${ }^{5}$ ic interpret coordinates to vector

Primary Method : Give 1 mark for each •

$$
12-6
$$

- $\overrightarrow{D B}=6-3$

$$
0-9
$$

$\bullet \quad \overrightarrow{D F}=\frac{2}{3} \overrightarrow{D B}$
-3 $\overrightarrow{D F}=\frac{2}{3} \begin{gathered}6 \\ 3 \\ -9\end{gathered} \begin{gathered}4 \\ 2 \\ -6\end{gathered}$

- $\quad \mathrm{D}=(6,3,9)$ so $\mathrm{F}=(10,5,3) \quad$ [Note 1] 4 marks
$\bullet \begin{array}{r}\text { •5 } \\ \overrightarrow{A F} \\ 3\end{array} \quad 1$ mark

Notes
1 Do not penalise candidates who write the coordinates of F as a column vector (treat as bad form).

2 A correct answer to (a) with no working may be awarded one mark only.

3 For guessing the coordinates of $F$, no marks should be awarded in (a).
1 mark is still available in (b) provided the guess in $(a)$ is geographically compatible with the diagram

$$
\begin{array}{ll}
\text { ie } & 0 \leq x \leq 12 \\
& 3 \leq y \leq 6 \\
& 0 \leq z \leq 9
\end{array}
$$

$4 \quad \ln (\mathrm{a})$
Where the ratio has been reversed (ie 1:2) leading to $\mathrm{F}=(8,4,6)$ then 3 marks may be awarded $(\cdot 1, \cdot 3, \cdot 4)$.
$5 \ln (b)$
Accept $\overrightarrow{A F}=-2 i+5 j+3 k$ for $\cdot 5$.

## Alternative Method 1 [Marks 1-4]

$$
\begin{array}{cc}
\bullet & \overrightarrow{D F}=2 \overrightarrow{F B} \\
\bullet^{2} & \boldsymbol{f}-\boldsymbol{d}=2 \boldsymbol{b}-2 \boldsymbol{f} \\
12 & 6 \\
\bullet^{3} & 3 \boldsymbol{f}=2 \begin{array}{c}
2 \\
6
\end{array} \\
0 & 9 \\
\bullet^{4} & \mathrm{~F}=(10,5,3) \\
{[\text { Note 1] }}
\end{array}
$$

## Alternative Method 2 [Marks 1-4]



## Alternative Method 3 [Marks 1-5]

$\bullet \quad \overrightarrow{A F}=\overrightarrow{A B}+\overrightarrow{B F}$
$\bullet \quad \overrightarrow{A F}=\overrightarrow{A B}+\frac{1}{3} \overrightarrow{B D}$

- $\overrightarrow{A F}=\begin{aligned} & 0 \\ & 6 \\ & 0\end{aligned}+\frac{1}{3} \begin{array}{rr}6 & 12 \\ 3 & - \\ 9 & 6\end{array}$
-2
- $\overrightarrow{A F}=5$

3

- ${ }^{5} \quad(\mathrm{~A}=(12,0,0$ so $) \mathrm{F}=(10,5,3)$

Alternative Method 4 [Marks 1-4]

| $x$ | 6 |  | 10 | 12 | $\bullet 1$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| y | 3 | - | 5 | 6 | -2 |
| z | 9 | - | 3 | 0 | $\bullet 3$ |
| so $\mathrm{F}=(10,5,3)$ |  |  |  |  | $\bullet 4$ |

4 Functions $f(x)=3 x-1$ and $g(x)=x^{2}+7$ are defined on the set of real numbers.
(a) Find $h(x)$ where $h(x)=g(f(x))$.
(b) (i) Write down the coordinates of the minimum turning point of $y=h(x)$.
(ii) Hence state the range of the function $h$.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 | a | 2 | C | A4 | NC | $05 / 7$ |
|  | b | 2 | C | A1 | NC |  |

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- ${ }^{1}$ ic interpret comp. function build-up
- ${ }^{2}$ ic interpret comp. function build-up
- ${ }^{3}$ ic interpret function
$\bullet$ ic interpret function

Primary Method : Give 1 mark for each •

- $\quad g(3 x-1) \quad$ stated or implied by $\cdot 2$
- ${ }^{2}(3 x-1)^{2}+7$

2 marks

- ${ }^{3} \quad \frac{1}{3}, 7$
[Note 1]
- ${ }^{4} \quad y \geq 7$
[Note 2]
2 marks


## Notes

1 For - 3
No justification is required for $\cdot 3$. Candidates may choose to dfferentiate etc but may still only earn one mark for a correct answer.

2 For $\cdot 4$
Accept $y>7, h \geq 7, h>7, h(x)>7, h(x) \geq 7$
Do not accept $x \geq 7, x>7$

## Common Error No. 1

$$
\begin{array}{lll}
\bullet^{1} & \times & f\left(x^{2}+7\right) \\
\bullet^{2} & \times \boldsymbol{V} & 3 x^{2}+20
\end{array}
$$

$$
\bullet \quad \times \sqrt{ } \quad(0,20)
$$

$$
\bullet^{4} \quad \times \sqrt{ } \quad y \geq 20
$$

$$
\text { award } 3 \text { marks }
$$

Notes $1 \& 2$ apply.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5 |  | 2 | A | C20, C21 | CN | $05 / 28$ |

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- ${ }^{1} \quad$ pd start differentiation process
- ${ }^{2}$ pd use the chain rule

Primary Method : Give 1 mark for each •

- $\quad 4(1+2 \sin (x))^{3}$
- $2 . \times 2 \cos (x)$

2 marks

## Common Error 1

- $\quad \times \quad 1+2 \sin ^{4}(x)$
$\bullet \quad \times \sqrt{ } \quad 8 \sin ^{3}(x) \times \cos (x)$ award 1 mark


## Common Error 2

$$
\begin{array}{lll}
\bullet & \times & 1+16 \sin ^{4}(x) \\
\bullet & \times \sqrt{ } & 64 \sin ^{3}(x) \times \cos (x) \\
& \text { award } & 1 \text { mark }
\end{array}
$$

## Common Error 3

[mixture of differentiating and integrating]
$\bullet^{1} \times \frac{1}{4}(1+2 \sin (x))^{3}$

- ${ }^{2} \times \quad \times \frac{1}{2} \cos (x)$
award 0 marks


## Common Error 4

- ${ }^{1} \times 4(1+2 \sin (x))^{5}$
$\bullet^{2} \times \sqrt{ } \times 2 \cos (x)$
award 1 mark

6 (a) The terms of a sequence satisfy $u_{n+1}=k u_{n}+5$. Find the value of $k$ which produces a sequence with a limit of 4 .
(b) A sequence satisfies the recurrence relation $u_{n+1}=m u_{n}+5, u_{0}=3$.
(i) Express $u_{1}$ and $u_{2}$ in terms of $m$.
(ii) Given that $u_{2}=7$, find the value of $m$ which produces a sequence with no limit.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | a | 2 | C | A13 | CN | $05 / 42$ |
|  | b | 5 | B | A11, A13 | CN |  |

The primary method $\mathrm{m} / \mathrm{s}$ is based on the following generic $\mathrm{m} / \mathrm{s}$. THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME

- ${ }^{1}$ ss know how to find limit
- ${ }^{2}$ pd process
- ${ }^{3}$ ic interpret rec. relation
- ${ }^{4}$ ic interpret rec. relation
$\bullet$ pd arrange in standard form
- ${ }^{6}$ pd process a quadratic
$\bullet^{7}$ ic use limit condition


## Notes

for (a)
1 Guess and Check
Guessing $k=-0.25$ and checking algebraically or iteratively that this does yield a limit of 4 may be awarded 1 mark.

2 No working
Simply stating that $k=-0 \cdot 25$ earns no marks.
3 Wrong formula
Work using an incorrect 'formula' leading to a valid value of $k$ (ie $|k|<1$ ) may be awarded 1 mark.
for (b)
4 If $\boldsymbol{u}_{\mathbf{2}}$ is not a quadratic, then no further marks are available.
5 An " $=0$ " must appear at least once in working at the $\cdot 5 / \cdot 6$ stage.

6 For candidates who make errors leading to no values outside the range $-1<m<1$, or to two values outside the range, then they must say why they are accepting or rejecting in order to gain $\bullet^{7}$

7 For $\cdot 7$, either crossing out the " $1 / 3$ " or underlining the " -2 " is the absolute minimum communication required for this $\mathrm{i} / \mathrm{c}$ mark. [A statement would be preferable]

Primary Method : Give 1 mark for each •

- ${ }^{1} \quad$ e.g. $4=k \times 4+5$
[Notes 1,2,3]
- $\quad k=-\frac{1}{4}$
-3 $u_{1}=3 m+5$
-4 $u_{2}=m(3 m+5)+5$
[Note 4]
$(m(3 m+5)+5=7)$
- ${ }^{5} 3 m^{2}+5 m-2=0$
[Note 5]
- ${ }^{6}(3 m-1)(m+2)=0$
- ${ }^{7} \quad m=-2$

5 marks

## Alternative Method 1 for (a)

$$
\begin{aligned}
& \text { Using } L=\frac{b}{1-a} \\
& \bullet^{1} \quad 4=\frac{5}{1-k} \\
& \bullet^{2} \quad k=-\frac{1}{4}
\end{aligned}
$$

## Alternative Method 2 for (a)

$$
\begin{aligned}
& L=k L+5 \\
& k L=L-5 \\
\bullet & k=\frac{L-5}{L} \\
\bullet & k=\frac{4-5}{4}=-\frac{1}{4}
\end{aligned}
$$

## Common Error 1

- ${ }^{1} \times 4=\frac{5}{1-a}$
$\bullet^{2} \quad \times \sqrt{ } a=-\frac{1}{4}$
award 1 mark


## Common Error 2

| $\sqrt{ } u_{1}=3 m+5$ |  |
| :---: | :---: |
| - ${ }^{4} \times u_{2}=3 m^{2}+5$ |  |
| - ${ }^{5} \times 3 m^{2}=2$ | or equivalent |
| ) $\times m=\sqrt{\frac{2}{3}}$ | (eased) |
| $\times \sqrt{ }$ there are do not yi | es which nit |
|  |  |

$7 \quad$ The function $f$ is of the form $f(x)=\log _{b}(x-a)$.
The graph of $y=f(x)$ is shown in the diagram.
(a) Write down the values of $a$ and $b$.
(b) State the domain of $f$.


| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 7 | a | 2 | C | A7 | NC | $05 / 9$ |
|  | b | 1 | C | A1 | NC |  |

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- ic interpret the translation
- ${ }^{2}$ ic interpret the base
- domain is $x>a \quad$ [Note 2]

1 mark

## Notes

$1 \quad$ No justification is required for marks 1 and 2.
BUT simply stating
$0=\log _{b}(5-a)$ and $1=\log _{b}(9-a)$
with no further work earns no marks.

However
$1=\log _{b}(9-a)$ and $b=9-a$
may be awarded 1 mark.
Of course to gain the other mark, both values would need to be stated.

2 Clearly $x>4$ is correct
but do not accept a domain of $x \geq 4$.

8 A function $f$ is defined by the formula $f(x)=2 x^{3}-7 x^{2}+9$ where $x$ is a real number.
(a) Show that $(x-3)$ is a factor of $f(x)$, and hence factorise $f(x)$ fully.
(b) Find the coordinates of the points where the curve with equation $y=f(x)$ crosses
the $x$ - and $y$-axes.
(c) Find the greatest and least values of $f$ in the interval $-2 \leq x \leq 2$.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 8 | a | 5 | C | A21 | NC | $05 / 10$ |
|  | b | 2 | C | A21 | NC |  |
|  | c | 5 | B | C11 | NC |  |

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- ${ }^{1}$ ss know to use $x=3$
- ${ }^{2}$ pd complete strategy
-3 ic interpret zero remainder
- ${ }^{4}$ ic interpret quadratic factor
$\bullet$ pd complete factorising
Primary Method : Give 1 mark for each •

| $\bullet \bullet^{1}$ | eg | 32 -7 0 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\bullet^{2}$ | eg | 32 -7 <br> 6  | 0 <br> -3 | -9 |
| 2 | -1 | -3 | 0 |  |

-3 remainder is zero so $(x-3)$ is a factor [Note 1]

- ${ }^{4} 2 x^{2}-x-3$
- $\quad(x-3)(2 x-3)(x+1) \quad$ stated explicitly $\quad 5$ marks


## Notes

In the Primary method, (a)
1 Candidates must show some acknowledgement of the result of the synthetic division. Although a statement w.r.t. the zero is preferable, accept something as simple as "underlining" the zero.

2 Candidates may use a second synthetic division to complete the factorisation. $\cdot 4$ and $\cdot 5$ are available.

## Alternative method 1 (marks 1-5) (linear factor by substitution)

- ${ }^{1} \quad f(3)=\ldots$
- ${ }^{2} f(3)=2 \times 3^{3}-7 \times 3^{2}+9=54-63+9=0$
$\bullet^{3} \quad$ eg 3

| 2 | -7 | 0 | 9 |
| :--- | :--- | :--- | :--- |
|  | 6 |  |  |
| 2 | -1 | -3 | 0 |

- ${ }^{4} \quad 2 x^{2}-x-3$
- $\quad(x-3)(2 x-3)(x+1)$

Alternative method 3 (marks 1-5) (quad factor by inspection)

- ${ }^{1} \quad f(3)=\ldots$
- $\quad f(3)=2 \times 3^{3}-7 \times 3^{2}+9=54-63+9=0$
- $\quad(x-3)\left(2 x^{2}\right.$ $\qquad$
- $\quad(x-3)\left(2 x^{2}-x-3\right)$
- $\quad(x-3)(2 x-3)(x+1)$


## Alternative method 2 (marks 1-5) (long division)

$$
\begin{aligned}
& \text { - }{ }^{5}(x-3)(2 x-3)(x+1)
\end{aligned}
$$

8 A function $f$ is defined by the formula $f(x)=2 x^{3}-7 x^{2}+9$ where $x$ is a real number.
(a) Show that $(x-3)$ is a factor of $f(x)$, and hence factorise $f(x)$ fully.
(b) Find the coordinates of the points where the curve with equation $y=f(x)$ crosses the $x$ - and $y$-axes.
(c) Find the greatest and least values of $f$ in the interval $-2 \leq x \leq 2$.

- ${ }^{6}$ ic interpret $y$-intercept
- ${ }^{7}$ ic interpret $x$-intercepts
- ${ }^{8}$ ss set derivative to zero
- ${ }^{9}$ pd solve
- ${ }^{10}$ ss evaluate function at an end point
- ${ }^{11}$ ic interpret results
- ${ }^{12}$ ic interpret results


## Primary Method : Give 1 mark for each -

- ${ }^{6} \quad(0,9)$
- ${ }^{7}(-1,0),\left(\frac{3}{2}, 0\right),(3,0) \quad$ [Note 3] 2 marks
- $8 x^{2}-14 x=0$
- ${ }^{9} \quad x=0$ or $x=\frac{14}{6}$
[Note 6]
$f(-2)=-35$ OR $f(2)=-3$
greatest value $=9$
${ }^{12}$ least value $=-35$
[Note 7]


## Notes

In the Primary method (b)

3 Only coordinates are acceptable for full marks.
Simply stating the values at which it cuts the $x$ - and $y$ axes may be awarded 1 mark (out of 2).

4 If all the coordinates are "round the wrong way" award 1 mark.

5 If the brackets are missing, treat as bad form.

In the Primary method (c)
6 Ignore any attempt to evaluate function at $X=7 / 3$.
$7 \cdot 11$ and $\cdot 12$ are not available unless both end points and the st. points have been considered.

In the Alt. 5 method (c)
$8 \cdot 12$ is not available unless both end points have been considered.

In (c)
9 Some candidates simply draw up a table using integer values from -2 to 2 and make conclusions from it. This earns $\cdot 9$ (Primary) ONLY, provided that one of the end points is correct.

9 If $\cos (2 x)=\frac{7}{25}$ and $0<x<\frac{\boldsymbol{\pi}}{2}$, find the exact values of $\cos (x)$ and $\sin (x)$.

|  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| 9 |  | 4 | C | T8 | NC | $05 / 16$ |

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THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE
GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE
THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME

- ${ }^{1}$ ss use double angle formula
- 2 pd process
- ${ }^{3}$ pd process
- ${ }^{4}$ pd process


## Notes

1 In the event of $\cos ^{2}(x)-\sin ^{2}(x)$ being used, no marks are available until the equation reduces to a quadratic in either $\cos (x)$ or $\sin (x)$.
$2 \cos (x)= \pm \frac{4}{5}, \sin (x)= \pm \frac{3}{5}$ loses $\cdot 3$.
$3 \cdot 3$ and $\cdot 4$ are only available as a consequence of attempting to apply the double angle formula. (This note does note apply to alt. method 2)

4 Guess and Check.
For guessing that $\cos (x)=\frac{4}{5}$ and $\sin (x)=\frac{3}{5}$,
substituting them into any valid expression for $\cos (2 x)$ and getting $7 / 25$, award 1 mark only.

Primary Method : Give 1 mark for each •
$2 \cos ^{2}(x)-1=\frac{7}{25}$
$\cos ^{2}(x)=\frac{32}{50}$
$\cos (x)=\frac{4}{5}$

- $\quad \sin (x)=\frac{3}{5}$


## Alternative Method 1

- $1-2 \sin ^{2}(x)=\frac{7}{25}$
- $\quad \sin ^{2}(x)=\frac{18}{50}$
- ${ }^{3} \quad \sin (x)=\frac{3}{5}$
- $\quad \cos (x)=\frac{4}{5}$


## Alternative Method 2

- $\quad(7,24,25)$ triangle $a+b=24$ and angle bisector $\quad \frac{a}{b}=\frac{7}{25}$
- $\quad a+\frac{25}{7} a=24 \quad a=\frac{21}{4}$
- $(21,28,35)$ triangle $t=\frac{35}{4}$


7

- ${ }^{4} \cos (x)=\frac{4}{5}$ and $\sin (x)=\frac{3}{5}$

Common Error 1
$2 \cos ^{2}(x)-1=\frac{7}{25}$
$\cos ^{2}(x)=\frac{64}{25}$
$\cos (x)=\frac{8}{5}$
$\sin (x)=\frac{6}{5}$
$\bullet 1 \sqrt{ } \bullet^{2} \times, \bullet^{3} \times, \bullet^{4} \times$
award 1 mark only

Common Incompletion 1

- $\sqrt{1} 2 \cos ^{2}(x)-1=\frac{7}{25}$
- ${ }^{2} \sqrt{ } \cos ^{2}(x)=\frac{32}{50}$
- $\times \cos (x)=\sqrt{\frac{32}{50}}$
- $\quad \times \sqrt{ } \sin (x)=\sqrt{\frac{18}{50}}$
award 3 marks

10 (a) Express $\sin (x)-\sqrt{3} \cos (x)$ in the form $k \sin (x-a)$ where $k>0$ and $0 \leq a \leq 2 \pi$. 4
(b) Hence, or otherwise, sketch the curve with equation $y=3+\sin (x)-\sqrt{3} \cos (x)$ in the interval $0 \leq x \leq 2 \boldsymbol{\pi}$.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 10 | a | 4 | C | T13 | NC | $05 / 27$ |
|  | b | 5 | A | T15 | NC |  |

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- ${ }^{1}$ ic expand
$\bullet^{2}$ ic compare coefficients
- ${ }^{3}$ pd process $k$
- ${ }^{4}$ pd process angle
- ${ }^{5}$ ic state equation
${ }^{6}$ ic completing graph
$\bullet^{7}$ ic completing graph
$\bullet$ ic completing graph
$\bullet$ ic completing graph


## Notes

In the whole question
Do not penalise more than once for not using radians.
In (a)
$1 \quad k(\sin (x) \cos (a)-\cos (x) \sin (a))$ is acceptable for $\cdot 1$
2 No justification is required for $\cdot 3$
$3 \quad \cdot{ }^{3}$ is not available for an unsimplified $\sqrt{ } 4$

4
$2(\sin (x) \cos (a)-\cos (x) \sin (a))$
. or $2 \sin (x) \cos ($ a $)-2 \cos (x) \sin ($ a $)$ is acceptabe for $\cdot 1$ and $\cdot \mathbf{3}$

5 Candidates may use any form of the wave equation to start with as long as their final answer is in the form $k \sin (x-a)$. If it is not, then ${ }^{4}$ is not available.
$6 \quad \cdot 4$ is only available for an answer in radians.

7 Treat $k \sin (x) \cos ($ a $)-\cos (x) \sin ($ a $)$ as bad form only if $\cdot \mathbf{2}$ is gained.

In (b)
8 The correct sketch need not include annotation of max, min or intercept for $\cdot 5$ to be awarded but you would need to see the graph lying between $y=1$ and $y=5$.
$9 \cdot 6$ is available for one cycle of any sinusoidal curve of period $2 \pi$ except $y=\sin (x)$. Some evidence of a scale is required.

10 For $\cdot 7$, accept $1 \cdot 3$ in lieu of $3-\sqrt{3}$
11 Do not penalise graphs which go beyond the interval $0 \ldots 2 \pi$.

Primary Method : Give 1 mark for each •

- ${ }^{1} \quad k \sin (x) \cos (a)-k \cos (x) \sin (a)$
- $\quad k \cos (\mathbf{a})=1, k \sin (\mathbf{a})=\sqrt{3}$


## STATED EXPLICITLY

 STATED EXPLICITLY- ${ }^{3} \quad k=2$
- $\quad a=\frac{\pi}{3}$
$\bullet^{5} y=3+2 \sin x-\frac{\pi}{3} \quad$ stated or implied by a correct sketch [Note 8]
a sketch showing
[Notes 9,10]
a sinusoidal curve
-7 $y$-intercept at $(0,3-\sqrt{3})$ and no $x$-intercepts
- 8 max at $\frac{5 \pi}{6}, 5$
$\min$ at $\frac{11 \pi}{6}, 1$


## Alternative marking for $\cdot 8$ and $\cdot 9$

$\bullet^{8} \max$ at $x=\frac{5 \pi}{6}$ and min at $x=\frac{11 \pi}{6}$
$\bullet{ }^{9} \quad$ graph lies between $y=1$ and $y=5$

## Alternative method for $\cdot 5$ to $\cdot 9$ (Calculus)

- $\frac{d y}{d x}=\cos (x)+\sqrt{3} \sin (x)=0$
- ${ }^{6} \tan (x)=-\frac{1}{\sqrt{3}}$
- ${ }^{7} \max \boldsymbol{a t}\left(\frac{5 \pi}{6}, 5\right)$
$\bullet^{8} \quad \min a t\left(\frac{11 \pi}{6}, 1\right)$
$\bullet^{9} \quad x=0 \quad y=3-\sqrt{3}$
and annotated sketch.


11 (a) A circle has centre $(t, 0), t>0$, and radius 2 units. Write down the equation of the circle.
(b) Find the exact value of $t$ such that the line $y=2 x$ is a tangent to the circle.


| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11 | a | 1 | C | G10 | CN | $05 / 28$ |
|  | b | 4 | A | G13 | CN |  |

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- ${ }^{1}$ ic state equ. of circle
- ${ }^{2}$ ss substitute
- ${ }^{3} \mathrm{pd}$ rearrange in standard form.
- $\quad$ ss know to use "discriminant $=0$ "

Primary Method : Give 1 mark for each •


## Notes

1 Subsequent to trying to use an expression masquerading as the discriminant e.g. $a^{2}-4 b c=0$, only $\cdot 5$ (from the last two marks) is still available.

2 Treat $t= \pm \sqrt{ } 5$ as bad form.

## Common Error No. 1

$$
\begin{gathered}
\bullet \quad \times \quad a=5, b=-2, c=t^{2}-4 \\
\bullet \\
4-20\left(t^{2}-4\right)=0 \\
20 t^{2}=84 \\
\times \sqrt{ } t=\sqrt{\frac{21}{5}} \text { or } \sqrt{4.2}
\end{gathered}
$$

## Alternative Method 1 (for (b))

Let $P$ be point of contact, $C$ the centre of the circle. Consider triangle OPC.

- $O P C=90^{\circ} \quad$ (tgt/radius)
- $P C=2$ (radius)
- $C P / O P=\tan (C O P)=2($ gradient of tgt $)$
- Hence $O P=1$
- and, by Pythagoras, $t=O C=\sqrt{ }\left(2^{2}+1^{2}\right)=\sqrt{ } 5$.


## Alternative Method 2 (for (b))

$$
y=2 x \quad m_{\operatorname{tgt}}=2 \text { and } m_{\mathrm{rad}}=-\frac{1}{2}
$$

- ${ }^{2}$ equ of radius is $x+2 y=t$
ie $x-t=-2 y$
- $\quad(-2 y)^{2}+y^{2}=4$
- $y=\frac{2}{\sqrt{5}}$
- ${ }^{5} \quad x=\frac{1}{2} y \quad x=\frac{1}{\sqrt{5}}$
- $\quad t=x+2 y \quad t=\sqrt{5}$
The boxplot shows the salaries of male and
[3] female graduates working for a large company at the end of their third year of employment.
Compare the salaries of these males and females.


Salaries (x £1000)

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| S1 |  | 3 | C | $4.1 .3 / 4$ | NC | $05 / 70$ |

```
-1 ic comment
\bullet ic comment
\bullet ic comment
```

Source
$05 / 70$

- ${ }^{1}$ one comment from list
- ${ }^{2}$ one comment from list
- ${ }^{3}$ one comment from list 3 marks males had higher salaries on average by $£ 2000$ range of salaries is broadly similar only 2 females achieved same salary as top $25 \%$ males majority of males earned more than the average female any other reasonable comment

S2 A bag contains 4 blue and 2 red counters. 2 counters are drawn at random without replacement.
The random variable $X$ is the number of blue counters drawn.
[5] (a) Find the probability distribution for $X$.
(b) Find $E(X)$.

| Qu. | part | marks | Grade | Syllabus Code | Calculator class | Source |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| S2 | 6 | C | $4.2 .11 / 12$ | NC | $05 / 22$ |  |

- ${ }^{1}$ ss know to find $\mathrm{P}(\mathrm{X}=0)$ etc
- ${ }^{2}$ pd process
- ${ }^{3}$ pd process
- ${ }^{4}$ pd process
- 5 ss choose correct form
- ${ }^{6}$ pd process

```
- \(\quad \frac{1}{15}\)
- \(\quad \frac{2}{6} \times \frac{4}{5}\)
- \(\quad \ldots+\frac{4}{6} \times \frac{2}{5}=\frac{8}{15}\)
- \(\frac{2}{5} \quad 4\) marks
- \({ }^{5} E(X)=x p(x)\)
- \({ }^{6} \frac{4}{3}\)


\section*{Mathematics Higher}

\section*{Instructions to Markers}
1. Marks must be assigned in accordance with these marking instructions. In principle, marks are awarded for what is correct, rather than marks deducted for what is wrong.
2. Award one mark for each 'bullet' point. Each error should be underlined in RED at the point in the working where it first occurs, and not at any subsequent stage of the working.
3. The working subsequent to an error must be followed through by the marker with possible full marks for the subsequent working, provided that the difficulty involved is approximately similar. Where, subsequent to an error, the working is eased, a deduction(s) of marks(s) should be made.

This may happen where a question is divided into parts. In fact, failure to even answer an earlier section does not preclude a candidate from assuming the result of that section and obtaining full marks for a later section.
4. Correct working should be ticked \((\checkmark)\). This is essential for later stages of the SQA procedures. Where working subsequent to an error(s) is correct and scores marks, it should be marked with a crossed tick ( \(\boldsymbol{X}\) or \(\boldsymbol{X} \checkmark\) ). In appropriate cases attention may be directed to work which is not quite correct (eg bad form) but which has not been penalised, by underlining with a dotted or wavy line.

Work which is correct but inadequate to score any marks should be corrected with a double cross tick (
5. - The total mark for each section of a question should be entered in red in the outer right hand margin, opposite the end of the working concerned.
- Only the mark should be written, not a fraction of the possible marks.
- These marks should correspond to those on the question paper and these instructions.
6. It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

Where a candidate has scored zero marks for any question attempted, " 0 " should be shown against the answer.
7. As indicated on the front of the question paper, full credit should only be given where the solution contains appropriate working. Accept answers arrived at by inspection or mentally where it is possible for the answer so to have been obtained. Situations where you may accept such working will normally be indicated in the marking instructions.
8. Do not penalise:
- working subsequent to a correct answer
- legitimate variations in numerical answers
- correct working in the "wrong" part of the question
- omission of units
- bad form
9. No piece of work should be scored through without careful checking - even where a fundamental misunderstanding is apparent early in the answer. Reference should always be made to the marking scheme - answers which are widely off-beam are unlikely to include anything of relevance but in the vast majority of cases candidates still have the opportunity of gaining the odd mark or two provided it satisfies the criteria for the mark(s).
10. If in doubt between two marks, give an intermediate mark, but without fractions. When in doubt between consecutive numbers, give the higher mark.
11. In cases of difficulty covered neither in detail nor in principle in the Instructions, attention may be directed to the assessment of particular answers by making a referral to the PA. Please see the general instructions for PA referrals.
12. No marks should be deducted at this stange for careless or badly arranged work. In cases where the writing or arrangement is very bad, a note may be made on the upper left-hand corner of the front cover of the script.
13. Transcription errors: In general, as a consequence of a transcription error, candidates lose the opportunity of gaining either the first ic mark or the first pd mark.
14. Casual errors: In general, as a consequence of a casual error, candidates lose the opportunity of gaining either the first ic mark or the first pd mark.
15. Do not write any comments on the scripts. A revised summary of acceptable notation is given on page 4 .

\section*{Summary}

Throughout the examination procedures many scripts are remarked. It is essential that markers follow common procedures:
1. Tick correct working.
2. Put a mark in the right-hand margin to match the marks allocations on the question paper.
3. Do not write marks as fractions.
4. Put each mark at the end of the candidate's response to the question.
5. Follow through errors to see if candidates can score marks subsequent to the error.
6. Do not write any comments on the scripts.

\section*{Remember - No comments on the scripts. Please use the following and nothing else.}
_ \(\boldsymbol{x} \quad\) The cross and underline. Underline an error and place a cross at the end of the line.
\(X \quad\) The tick-cross. Use this to show correct or \(\boldsymbol{X} \boldsymbol{\checkmark} \quad\) work where you are following through subsequent to an error.

The roof. Use this to show something is missing such as a crucial step in a proof of a 'condition' etc.


The tilde. Use this to indicate a minor transgression which is not being penalised (such as bad form).
*
The double-cross tick. Use this to show correct work but which is inadequate to score any marks. This may happen when working has been eased.

Bullets showing where marks have been allotted may be shown on scripts


Remember - No comments on the scripts. No abbreviations. No new signs.
Please use the above and nothing else.
All of these are to help us be more consistent and accurate.
Note: There is no such thing as a transcription error, a trivial error, a casual error or an insignificant error. These are all mistakes and as a consequence a mark is lost.

1 Find \(\int \frac{4 x^{3}-1}{x^{2}} d x, x \neq 0\).
\begin{tabular}{|lllllll|}
\hline Qu. part & marks & Grade & Syllabus Code & Calculator class & Source \\
1 & & 4 & C & C14, C13 & CN & \(05 / 20\) \\
\hline
\end{tabular}

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- \({ }^{1}\) ss: arrange in integrable form
- \({ }^{2}\) pd: integrate positive index
-3 pd: integrate negative index
- \({ }^{4}\) ic: complete including const. of int.

Primary Method : Give 1 mark for each -
- \({ }^{1} 4 x-x^{-2}\)
- \(2 \frac{4 x^{2}}{2}\)
- \({ }^{3}-\frac{x^{-1}}{-1}\)
- \(42 x^{2}+x^{-1}+c\)
[Note 3]

\section*{Notes}

1 If incorrectly expressed in integrable form, follow throughs must match the generic marking scheme.
\(2 \cdot 3\) can only be awarded on follow through provided the integral involves a negative index.
3.4 can only be awarded if the constant of integration appears somewhere in the working.
\(4 \cdot 4\) can only be awarded as a result of at least one valid integration at the \(\cdot \mathbf{2}\) or \(\cdot \mathbf{3}\) stage.

Common Error 1
\[
\begin{aligned}
& { }^{1} \times \quad 4 x-1 \\
& \text { - }{ }^{2} \times \sqrt{ } \quad 2 x^{2} \\
& \bullet^{3} \times-x \quad\left[\text { see Generic } \bullet^{3}\right] \\
& \text { - }{ }^{4} \times \sqrt{ } \quad 2 x^{2}-x+c \\
& \text { a w a r d } 2 \text { m a }
\end{aligned}
\]

Common Error 2
\[
\begin{array}{|llll}
\hline \bullet^{1} & \times & 4 x^{3}-1-x^{-2} \\
\bullet & \times \sqrt{ } & \frac{4 x^{4}}{4}-x \\
\bullet^{3} & \times \sqrt{ } & -\frac{x^{-1}}{-1} \\
\bullet^{4} & \times \sqrt{ } & x^{4}-x+x^{-1}+c \\
\mathrm{k} & & & \\
\mathrm{a} & \mathrm{w} & \mathrm{a} & \mathrm{r} \\
\mathrm{~s} & \mathrm{~d} & 3 & \mathrm{~m}
\end{array} \mathrm{a}
\]

Common Error 3


Common Error 4


Common Error 5


Common Error 6
s

Throughout this paper, unless specifically mentioned, a correct answer with no working receives no credit.

2 Triangles ACD and BCD are right-angled at D with angles \(p\) and \(q\) and lengths as shown in the diagram.
(a) Show that the exact value of \(\sin (p+q)\) is \(\frac{84}{85}\).
(b) Calculate the exact values of
(i) \(\quad \cos (p+q)\)
(ii) \(\tan (p+q)\).

\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
2 & a & 4 & C & T9 & CN & \(05 / 41\) \\
& b & 3 & C & T9 & CN & \\
\hline
\end{tabular}

The primary method \(\mathrm{m} / \mathrm{s}\) is based on the following generic \(\mathrm{m} / \mathrm{s}\). THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME
- \({ }^{1}\) ic: interpret diagram
- \({ }^{2}\) ic: interpret diagram
- \({ }^{3} \quad\) ss: \(\quad\) expand \(\sin (\mathrm{A}+\mathrm{B})\)
- \({ }^{4}\) pd: sub. and complete
\(\bullet\) ss: expand \(\cos (\mathrm{A}+\mathrm{B})\)
- \({ }^{6}\) pd: sub. and complete
\(\bullet^{7}\) ic: use \(\tan (x)=\sin (x) / \cos (x)\)

\section*{Notes}
\(1 \cdot 1\) and \(\cdot 2\) may, if necessary, be awarded as follows
- \(\quad \sin (p)=\frac{15}{17}, \sin (q)=\frac{6}{10}\)
\(\bullet^{2} \quad \cos (p)=\frac{8}{17}, \cos (q)=\frac{8}{10}\)

2 For •4
There has to be some working to show the completion.
eg
\[
\ldots \ldots \ldots \ldots=\frac{120+48}{170}=\frac{168}{170}=\frac{84}{85}
\]
or
\[
\ldots \ldots \ldots \ldots=\frac{60}{85}+\frac{24}{85}=\frac{84}{85}
\]
or
\[
\ldots \ldots \ldots \ldots=\frac{12}{17}+\frac{24}{85}=\frac{84}{85}
\]

3 Calculating approx angles using invsin and invcos can gain no credit at any point.

4 Any attempt to use \(\sin (p+q)=\sin (p)+\sin (q)\) loses \(\cdot 3\) and \(\cdot 4\).
Any attempt to use \(\cos (p+q)=\cos (p)+\cos (q)\) loses \(\cdot 5\) and \(\cdot 6\).
This second option must not be treated as a repeated error.

Primary Method : Give 1 mark for each •
\(\bullet^{1} \quad \cos (p)=\frac{8}{17}, \sin (p)=\frac{15}{17}\left[\begin{array}{l}{[\text { Note 1] }} \\ \text { stated or implied by } \cdot 4 \text { when }\end{array}\right.\)
\(\bullet^{2} \quad \cos (q)=\frac{8}{10}, \sin (q)=\frac{6}{10} \quad\) written in the same order as \(\cdot \mathbf{3}\)
- \({ }^{3} \quad \sin (p) \cos (q)+\cos (p) \sin (q) \quad\) explicitly stated
- \(\frac{15}{17} \times \frac{8}{10}+\frac{8}{17} \times \frac{6}{10}=\&\) complete 4 marks
- \({ }^{5} \quad \cos (p) \cos (q)-\sin (p) \sin (q)\)
- \({ }^{6} \quad-\frac{13}{85}\) or equivalent fraction
\(\bullet^{7} \quad-\frac{84}{13}\) or equivalent fraction \(\left(\right.\) eg \(\left.-\frac{7140}{1105}\right)\)

\section*{Alternative 1 (for marks 3 \& 4)}
- \({ }^{3} \frac{21}{\sin (p+q)}=\frac{10}{\frac{8}{17}}\)
- \(10 \sin (p+q)=\frac{168}{17}\) and complete

\section*{Alternative 2 (for marks 5 \& 6)}
- \(\quad \cos (p+q)=\frac{17^{2}+10^{2}-21^{2}}{2.17 .10}\)
\(\bullet^{6} \quad-\frac{13}{85}\)

\section*{Alternative 3 (for marks 5 \& 6)}
- \(\cos ^{2}(p+q)=1-\left(\frac{84}{85}\right)^{2}\)
- \({ }^{6} \quad \cos (p+q)=-\frac{13}{85}\) with justification of the choice of negative sign e.g. \((15+6)^{2}(=441)>17^{2}+10^{2}(=389)\) or using the cosine rule

3 (a) A chord joins the points \(\mathrm{A}(1,0)\) and \(\mathrm{B}(5,4)\) on the circle as shown in the diagram. Show that the equation of the perpendicular bisector of chord AB is \(x+y=5\).
(b) The point C is the centre of this circle. The tangent at the point A on the circle has equation \(x+3 y=1\).
Find the equation of the radius CA.
(c) (i) Determine the coordinates of the point C.
(ii) Find the equation of the circle.


\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
3 & a & 4 & C & G7 & CN & \(05 / 44\) \\
& b & 4 & C & G15 & CN & \\
& c & 4 & C & G10 & CN & \\
\hline
\end{tabular}

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- \({ }^{1}\) ss: find perp. bisector
- \({ }^{2}\) pd: calc. perp. gradient
- \({ }^{3}\) ss: find approp. mid-point
- \({ }^{4}\) ic: complete proof
- 5 ss: compare with \(y=m x+c\)
- \({ }^{6}\) ic: state gradient
- \({ }^{7}\) ss: find gradient of radius
- 8 ic: state equation of line
- \({ }^{9}\) ss: solve sim. equations
- \({ }^{10} \mathrm{pd}\) : solve sim. equations
- \({ }^{11}\) ic: state equation of circle
- \({ }^{12}\) pd: calculate radius

\section*{Notes}

1 To gain \(\bullet 4\) some evidence of completion needs to be shown
eg
\[
\begin{aligned}
& y-2=-1(x-3) \\
& y-2=-x+3 \\
& y+x=5
\end{aligned}
\]
\(2 \cdot 4\) is only available if an attempt has been made to find and
use both a perpendicular gradient and a midpoint.
\(3 \cdot 8\) is only available if an attempt has been made to find and use a perpendicular gradient.

4 At the \(\cdot 9, \cdot 10\) stage
Guessing ( 2,3 ) (from stepping) and checking it lies on perp. bisector of AB may be awarded \(\cdot 9\) and \(\cdot 10\) Guessing ( 2,3 ) (with or without reason) and with no check gains neither \(\cdot 9\) nor \(\cdot 10\)

5 Solving \(y=3 x-3\) and \(x+3 y=1\) leading to \((1,0)\) will lose \(\cdot 9\) and \(\cdot 10\).

6 to gain \(\cdot 12\) some evidence of use of the distance formula needs to be shown.

7 At the \(\cdot 11\) and \(\cdot 12\) stage
Subsequent to a guess for the coordinates of \(C, \cdot 11\) and \(\cdot 12\) are only available if the guess is such that \(0<x<5\) and \(0<y<4\).


\section*{Primary Method : Give 1 mark for each -}
\[
m_{A B}=1
\]
\[
\bullet^{2} \quad m_{\perp}=-1
\]
\[
\bullet^{3} \quad \text { midpoint }=(3,2)
\]
\[
\text { - } y-2=-1(x-3) \text { a nconoplete } \quad[\text { Notes 1,2] } 4 \text { marks }
\]
\[
\bullet 5=-\frac{1}{3} x \ldots \ldots . \quad \text { stated/implied by } \cdot 6
\]
\[
\bullet^{6} \quad m_{t g t}=-\frac{1}{3}
\]
\[
\bullet^{7} \quad m_{\text {rad }}=3 \quad \text { stated } / \text { implied by } \cdot 8
\]
\[
\text { -8 } y-0=3(x-1) \quad \text { [Note 3] }
\]
\[
\bullet^{9} \quad \text { use } x+y=5
\]
\[
\text { a } \quad \mathrm{n} y=\mathrm{d} 3 x-3
\]
\[
\bullet^{10} \quad x=2, y=3
\]
\[
e^{11}(x-2)^{2}+(y-3)^{2}=r^{2}
\]
\[
\bullet^{12} r^{2}=10 \quad \text { [Note 6] }
\]

\section*{Alternative 1 [for -9 and -10]}
- \({ }^{9} \quad \mathrm{D}=(3,6)\) where D is intersection of the perp. to AB through B and the circle.
\({ }^{10} \mathrm{C}=\) midpoint of \(\mathrm{AD}=(2,3)\)

\section*{Common Error 1 [ for \(\cdot 5\) to 8 ]}
\[
\begin{aligned}
& 3 y=-x+1 \\
& m=-1 \\
& m_{r a d}=1 \\
& y-0=1(x-1) \\
& \bullet 5 \times \quad \bullet 6 \times \quad \bullet 7 \times \text { eased } \quad \bullet 8 \times \sqrt{ } \\
& \text { a w a r d } 1 \text { m a r } k
\end{aligned}
\]

Common Error 2 [ for \(\cdot 5\) to \(\cdot 8\) ]
\(x+3 y=1\) so \(m=3\)
\(y-0=3(x-1)\)
a w a r d 0 macr m

4 The sketch shows the positions of Andrew(A), Bob (B) and \(\operatorname{Tracy}(\mathrm{T})\) on three hill-tops.
Relative to a suitable origin, the coordinates (in hundreds of metres) of the three people are \(\mathrm{A}(23,0,8), \mathrm{B}(-12,0,9)\) and \(\mathrm{T}(28,-15,7)\).
In the dark, Andrew and Bob locate Tracy using heat-seeking beams.

(a) Express the vectors \(\overrightarrow{\mathrm{TA}}\) and \(\overrightarrow{\mathrm{TB}}\) in component form.
(b) Calculate the angle between these two beams.
\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
4 & a & 2 & C & G17 & CN & \(05 / 55\) \\
& b & 5 & C & G28 & Ca & \\
\hline
\end{tabular}

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THIS GENERIC M/S MAY BE USED AS AN EQUIVALENCE
GUIDE BUT ONLY WHERE A CANDIDATE DOES NOT USE THE PRIMARY METHOD OR ANY ALTERNATIVE METHOD SHOWN IN DETAIL IN THE MARKING SCHEME
- \({ }^{1}\) ic: state vector components
\(\bullet\) ic: state vector components
- \({ }^{3} \mathrm{pd}\) : find length of vector
- \({ }^{4} \mathrm{pd}\) : find length of vector
- \({ }^{5}\) pd: find scalar product
- \({ }^{6}\) Ss: use scalar product
- \({ }^{7}\) pd: evaluate angle

\section*{Notes}

In (a)
For calculating \(\overrightarrow{A T}\) and \(\overrightarrow{B T}\) award 1 mark out of 2 .
2 Treat column vectors written like \((-40,15,2)\) as bad form.
In (b)
3 For candidates who do not attempt \(\cdot \mathbf{7}\), the formula quoted at -6 must relate to the labelling in the question for \(\cdot 6\) to be awarded.
4 Do not penalise premature rounding.

5 The use of \(\tan (A \hat{T} B)=\frac{\overrightarrow{T A} \cdot \overrightarrow{T B}}{\rightarrow \quad \rightarrow}\) loses \(\cdot 6\)
\[
|T A \| T B|
\]

6 The use of \(\cos (A \hat{T} B)=\frac{T A \cdot T B}{|\overrightarrow{A B}|}\) means that only \(\cdot 5\) and -7 are available.

Primary Method : Give 1 mark for each •
\[
\begin{aligned}
& \text { - } \quad \overrightarrow{T A}=\left(\begin{array}{c}
-5 \\
15 \\
1
\end{array}\right) \\
& \bullet \quad \overrightarrow{T B}=\left(\begin{array}{c}
-40 \\
15 \\
2
\end{array}\right) \\
& \text { - }{ }^{3} \quad|\overrightarrow{T A}|=\sqrt{251} \\
& \text { - } \quad|\overrightarrow{T B}|=\sqrt{1829} \\
& \text { •5 } \quad \text { TA.TB }=427 \\
& \bullet^{6} \quad \cos (A \hat{T} B)=\frac{\overrightarrow{T A \cdot T B}}{|\overrightarrow{T A}||\overrightarrow{T B}|} \\
& \text { stated or implied by } \cdot 7 \\
& \text { [Note 3] } \\
& 2 \text { marks }
\end{aligned}
\]

5 marks
\(\bullet^{7} \quad A \hat{T} B=50 \cdot 9^{\circ}\) OR \(0.889^{c} \quad\) [Note 4]
OR 56.6 grads
Alternative 1 for \({ }^{\bullet} \mathbf{3}\) to \({ }^{\bullet} 7\) (Cosine Rule)
-3 \(|\overrightarrow{T A}|=\sqrt{251}\)
\(\bullet|\overrightarrow{T B}|=\sqrt{1829}\)
- \(|\overrightarrow{A B}|=\sqrt{1226}\)
\({ }^{6} \quad \cos (A \hat{T} B)=\frac{1829+251-1226}{2 \cdot \sqrt{1829} \cdot \sqrt{251}} \quad\) stated or implied by \(\cdot 7\)
- \({ }^{7} \quad A \hat{T} B=50 \cdot 9^{\circ}\)

5 marks


4 The sketch shows the positions of Andrew(A), Bob (B) and \(\operatorname{Tracy}(\mathrm{T})\) on three hill-tops.
Relative to a suitable origin, the coordinates (in hundreds of metres) of the three people are \(\mathrm{A}(23,0,8), \mathrm{B}(-12,0,9)\) and \(\mathrm{T}(28,-15,7)\).
In the dark, Andrew and Bob locate Tracy using heat-seeking beams.

(a) Express the vectors \(\overrightarrow{\mathrm{TA}}\) and \(\overrightarrow{\mathrm{TB}}\) in component form.
(b) Calculate the angle between these two beams.

Common Error 1 : Finding angle BOA
u s. \(\overrightarrow{O B} \neq\left(\begin{array}{c}-12 \\ 9 \\ 9\end{array}\right)\) and \(\overrightarrow{O A}=\left(\begin{array}{c}23 \\ 0 \\ 8\end{array}\right)\)
- \(|\overrightarrow{O B}|=\sqrt{225}\) and \(|\overrightarrow{O A}|=\sqrt{593}\)
- \(\overrightarrow{O B} \cdot \overrightarrow{O A}=-204\)
- \(\cos (B \hat{O} A)=\frac{\overrightarrow{O B} \cdot \overrightarrow{O A}}{|\overrightarrow{O B} \| \overrightarrow{O A}|}\)
- \(\quad B \hat{O} A=124 \cdot 0^{\circ}\) OR \(2 \cdot 163^{c}\)
a wod alrma r r p e r b u l e t

\section*{Common Error 2 : Finding angle BOT}

\section*{Common Error 3 : Finding angle AOT}
u st \(\quad \overrightarrow{O A} \neq\left(\begin{array}{c}23 \\ 9 \\ 8\end{array}\right)\) and \(\overrightarrow{O T}=\left(\begin{array}{c}28 \\ -15 \\ 7\end{array}\right)\)
- \(|\overrightarrow{O A}|=\sqrt{593}\) and \(|\overrightarrow{O T}|=\sqrt{1058}\)
- \(O A . O T=700\)
- \(\left\langle\begin{array}{r}\cos (A \hat{O} T)=\frac{\overrightarrow{O A} \cdot \overrightarrow{O T}}{|\overrightarrow{O A}||\overrightarrow{O T}|} \\ A \hat{O} T=27 \cdot 9^{\circ}\end{array}\right\rangle\)
aw wd 1 macr \(\mathrm{m} \quad \mathrm{p}\) e r
Common Error 4 : Finding angle ABT
\(\mathbf{u} \quad \mathbf{s} \quad \overrightarrow{B A} \nRightarrow\left(\begin{array}{c}35 \\ \mathbf{g} \\ -1\end{array}\right)\) and \(\overrightarrow{B T}=\left(\begin{array}{c}40 \\ -15 \\ -2\end{array}\right)\)
- \(|\overrightarrow{B A}|=\sqrt{1226}\) and \(|\overrightarrow{B T}|=\sqrt{1829}\)
- \(\quad B A \cdot B T=1402\)
\(\bullet\left\langle\begin{array}{r}\cos (A \hat{B} T)=\frac{\overrightarrow{O A} \cdot \overrightarrow{O T}}{\overrightarrow{O A}|\overrightarrow{O T}|} \\ A \hat{B} T=20 \cdot 6^{\circ}\end{array}\right\rangle\)
a w a r d 1 marr

\section*{Common Error 5 : Finding angle BAT}
\(\mathrm{u} \quad \mathrm{s} \quad \overrightarrow{\mathrm{iAB}} \neq\left(\begin{array}{c}-35 \\ \mathrm{~g} \\ 1\end{array}\right)\) and \(\overrightarrow{A T}=\left(\begin{array}{c}5 \\ -15 \\ -1\end{array}\right)\)
- \(|\overrightarrow{A B}|=\sqrt{1226}\) and \(|\overrightarrow{A T}|=\sqrt{251}\)
- \(\overrightarrow{A B} \cdot \overrightarrow{A T}=-176\)
\(\bullet\left\langle\begin{array}{r}\cos (B \hat{A} T)=\frac{\overrightarrow{A B} \cdot \overrightarrow{A T}}{\overrightarrow{A B}| | \overrightarrow{A T} \mid} \\ B \hat{A} T=108 \cdot 5^{\circ}\end{array}\right\rangle\)


5 The curves with equations \(y=x^{2}\) and \(y=2 x^{2}-9\) intersect at K and L as shown.

Calculate the area enclosed between the curves.

\begin{tabular}{|lllllll|}
\hline \hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
5 & & 8 & C & C17 & CN & \(05 / 49\) \\
\hline
\end{tabular}

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- \({ }^{1}\) Ss: find intersection
\(\bullet{ }^{2}\) pd: process quadratic equ.
-3 ss: upper - lower
- \({ }^{4}\) ic: interpret limits
- \({ }^{5}\) pd: sub. \& simplify Upper - Lower
- \({ }^{6}\) pd: integrate
- \({ }^{7}\) ic: substitute limits
- \({ }^{8}\) pd: evaluate and complete

\section*{Primary Method : Give 1 mark for each \(\cdot\)}
- \(x^{2}=2 x^{2}-9\)
- \({ }^{2} \quad x= \pm 3\)
- 3 upper - lower [Notes 3,4] stated or implied by \(\cdot 5\)
- \({ }^{4}\) eg \(\int_{0}^{3} \ldots\)
- \(5 \quad x^{2}-2 x^{2}+9\)
- \({ }^{6}\left[-\frac{1}{3} x^{3}+9 x\right]_{0}^{3}\)
- \(\quad\left(-\frac{1}{3} \times 3^{3}+9 \times 3\right)-0\)
- \(2 \times 18=36 \quad\) [Note 3] 8 marks

\section*{Alternative 1 for \(\bullet^{4}\) to \({ }^{\bullet} 8\)}
\({ }^{4}\) eg \(\int_{-3}^{3} \ldots\)
- \({ }^{5} x^{2}-2 x^{2}+9\)
- \({ }^{6}\left[-\frac{1}{3} x^{3}+9 x\right]_{-3}^{3}\)
- \(7 \quad\left(-\frac{1}{3} \times 3^{3}+9 \times 3\right)-\left(-\frac{1}{3} \times(-3)^{3}+9 \times(-3)\right)\)
\(\bullet^{8} \quad 36\)

\section*{Alternative 2 for \({ }^{\bullet} \mathbf{3 ~ t o ~}^{\bullet} 8\)}
- \(\quad x=\frac{3}{2} \sqrt{2}\)

- \(\int_{0}^{\frac{3}{2} \sqrt{2}}\left(9-2 x^{2}\right) d x\) leading to \(\mathrm{B}=9 \sqrt{2}\)
- \(5 \quad \int_{0}^{3}\left(x^{2}\right) d x\) leading to \(\mathrm{A}+\mathrm{C}=9\)
- \(\quad \int_{\frac{3}{2} \sqrt{2}}^{3}\left(2 x^{2}-9\right) d x\) leading to \(\mathrm{C}=9 \sqrt{2}-9\)
- \({ }^{7} \quad A=18-9 \sqrt{2}(5.3)\)
- \({ }^{8} \quad\) Total area \(=36\)
\(6 \quad\) The diagram shows the graph of \(y=\frac{24}{\sqrt{x}}, x>0\).

Find the equation of the tangent at P , where \(x=4\).

\begin{tabular}{|llllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class \\
6 & & 6 & B & C5, C3 & Source \\
\hline
\end{tabular}

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- \({ }^{1}\) ss : know to differentiate
- \({ }^{2}\) ic : express in st. form
\(\bullet{ }^{3}\) pd : differentiate -ve fractional index
\({ }^{4}\) pd : evaluate -ve fractional index
\(\bullet{ }^{5} \mathrm{pd}\) : evaluate \(y\)-coord
\(\cdot{ }^{6}\) ic : state equ of tangent

\section*{Primary Method : Give 1 mark for each •}
- \(\quad \frac{d y}{d x}=\ldots\)
-2 \(y=24 x^{-\frac{1}{2}}\)
- \(\frac{d y}{d x}=-12 x^{-\frac{3}{2}}\)
- \(\frac{d y}{d x} x=4=-\frac{3}{2}\)
- \(5 y_{x=4}=12\)
\(\bullet^{6} y-12=-\frac{3}{2}(x-4) \quad[\) Notes \(1,2,3] \quad 6\) marks
\[
n r \quad[2 y+3 x=36]
\]
\(n r=\) not required

\section*{Notes}
1.4 and \(\cdot 6\) are only available if an attempt to find the gradient is based on differential calculus.
\(2 \cdot 6\) is not available to candidates who find and use a perpendicular gradient.
\(3 \cdot 6\) is only available for a numerical value of \(m\).

Common Error 1
- \(\quad \frac{d y}{d x}=\ldots\)
- \(2 y=24 x^{-\frac{1}{2}}\)
- \(\frac{d y}{d x}=\frac{24 x^{\frac{1}{2}}}{\frac{1}{2}}\)
- \(\frac{d y}{d x} x=4=96\)
- \(y_{x=4}=12\)
- \({ }^{6} y-12=96(x-4)\)
-1 \(\sqrt{ }\)
-2 \(\sqrt{ }\)
-3 \(\times\)
- \(4 \times \quad\) eased
\(\bullet 5 \sqrt{ }\)
-6 \(\times \sqrt{ }\)
a w a r d \(4 \quad \mathrm{~m}\) a

Common Error 2
\({ }^{-1}\)
- \({ }^{2} y=24 x^{-\frac{1}{2}}\)
- \(\int 24 x^{-\frac{1}{2}} d x=\frac{24 x^{\frac{1}{2}}}{\frac{1}{2}}+c\)
- \({ }^{4}\) gradient \(=96\)
- \({ }^{5} y_{x=4}=12\)
- \({ }^{6} y-12=96(x-4)\)
-1 \(\times\)
\(\bullet 2 \sqrt{ }\)
- \(3 \times\)
-4 \(\times\)
Note 1
\(\bullet 5 \sqrt{ }\)
-6 \(\times\)
Note 1

7 Solve the equation \(\log _{4}(5-x)-\log _{4}(3-x)=2, x<3\).
\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
7 & & 4 & A & A7 & CN & 0525 \\
\hline
\end{tabular}

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- \({ }^{1}\) ss: use the log laws
- \({ }^{2}\) ss: know to convert from log to expo
- \({ }^{3}\) pd: process conversion
- \({ }^{4}\) pd: find valid solution

\section*{Notes}

1 For •4
Accept answer as a decimal.

\section*{Common Error No. 1}
- \(1 \sqrt{ } \quad \log _{4}\left(\frac{5-x}{3-x}\right)=\log _{4}(8)\)
-2 \(\times\)
- \(3 \times\)
\[
\frac{5-x}{3-x}=8
\]
-4 \(\times \sqrt{ } \quad x=\frac{19}{7}\)
a w a r d 2 m a r \(k \quad\) s

\section*{Common Error No. 2}
- \(1 \quad \sqrt{ } \quad \log _{4}\left(\frac{5-x}{3-x}\right)=2\)
\(\bullet 2 \times \quad 4^{\frac{5-x}{3-x}}=2\)
-3 \(\times\)
\[
\frac{5-x}{3-x}=\frac{1}{2}
\]
-4 \(\times \sqrt{ } \quad x=7\) which is not a valid sol.
a w a r d 2 m a r k s

\section*{Common Error No. 3}
- \(1 \quad \sqrt{ } \quad \log _{4}\left(\frac{5-x}{3-x}\right)=2\)
- \(2 \times \quad \log _{4}\left(\frac{5-x}{3-x}\right)=\log _{4} 2\)
- \(3 \times \frac{5-x}{3-x}=2\)
-4 \(\times \sqrt{ } \quad x=1\).
a w a r d 2 mar m s

Primary Method : Give 1 mark for each -
- \(\log _{4}\left(\frac{5-x}{3-x}\right)\)
\(\bullet \quad\) use \(\log _{a}(b)=c \Leftrightarrow b=a^{c} \quad\) stated or implied by \(\cdot 3\)
- \(\frac{5-x}{3-x}=4^{2}\)

See Cave
- \(x=\frac{43}{15} \quad 4\) marks

Alternative 1
- \(\log _{4}\left(\frac{5-x}{3-x}\right)\)
- \(2 \quad 2 \log _{4} 4\)
stated or implied by -3
- \(3\left(\frac{5-x}{3-x}\right)=4^{2}\)
- \(\quad x=\frac{43}{15}\)

\section*{Cave}


\section*{8 Two functions, \(f\) and \(g\), are defined by}
\(f(x)=k \sin (2 x)\) and \(g(x)=\sin (x)\) where \(k>1\).
The diagram shows the graphs of
\(y=f(x)\) and \(y=g(x)\) intersecting at \(\mathrm{O}, \mathrm{A}, \mathrm{B}, \mathrm{C}\) and D. Show that, at A and C, \(\cos (x)=\frac{1}{2 k}\).

\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
8 & & 5 & A & T10 & CN & \(05 / 47\) \\
\hline
\end{tabular}

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- \({ }^{1}\) ss: equate for intersection
- \({ }^{2}\) ss: use double angle formula
- \({ }^{3} \mathrm{pd}\) : factorise
- \({ }^{4}\) pd: process two solutions
- \({ }^{5}\) ic: complete proof

\section*{Primary Method : Give 1 mark for each -}
- \({ }^{1} \quad k \sin (2 x)=\sin (x)\)
[Note 1]
- \({ }^{2} k \times 2 \sin (x) \cos (x)\)
- \({ }^{3} \quad \sin (x)(2 k \cos (x)-1)=0\)
- \({ }^{4} \quad \sin (x)=0\)
a \(\quad n \cos (d x)=\frac{1}{2 k}\)
\(\bullet^{5} \quad \sin (x)=0 \Rightarrow x=0, \pi, 2 \pi\)
i.e. at \((\mathrm{O}), \mathrm{B}\) and D
[Note 2]
a \(\quad \operatorname{ras}(\boldsymbol{d})=\frac{1}{2 k}\) is for A and C .

\section*{Notes}

1 Only \(\cdot 1\) is available for candidates who substitute a numerical value for \(k\) at the start.
\(2 \cdot 5\) is only available if a suitable comment regarding points ( \(O\) ), \(B\) and \(D\) is made.
3 If all the terms are transposed to one side, then an "=0" needs to appear at least once.

4 For Alternative 3
\(\cdot 4\) and \(\cdot 5\) are not available unless \(\cdot 3\) has been awarded.

\section*{Common Error 1}
- \({ }^{1} \quad \sqrt{ } \quad k \sin (2 x)=\sin (x)\)
\({ }^{2} \quad \sqrt{ } \quad k \times 2 \sin (x) \cos (x)-\sin (x)=0\)
- \({ }^{3} \sqrt{ } \quad \sin (x)(2 k \cos (x)-1)\)
- \(\times 2 k \cos (x)-1=0\)
- \({ }^{5} \times \cos (x)=\frac{1}{2 k}\) at A and C.
a \(w\) 3a r nol a r \(k \quad s\)

\section*{Common Error 2}
\[
\begin{array}{lll}
\bullet^{1} & \sqrt{ } & k \sin (2 x)=\sin (x) \\
\bullet^{2} & \sqrt{ } & k \times 2 \sin (x) \cos (x)=\sin (x) \\
\bullet^{3} & \times & k \times 2 \cos (x)=1 \\
\bullet & \times & \\
\bullet & \times & \cos (x)=\frac{1}{2 k} \text { at A and C. }
\end{array}
\]
\[
\begin{array}{llllllllll}
\text { a } & \text { w } & \text { a } & \mathrm{d} & 2 & \mathrm{~m} & \mathrm{r} & \mathrm{k} & \mathrm{~s}
\end{array}
\]
\(9 \quad\) The value \(V\) (in \(£\) million) of a cruise ship \(t\) years after launch is given by the formula \(V=252 e^{-0.06335 t}\).
(a) What was its value when launched?
(b) The owners decide to sell the ship once its value falls below \(£ 20\) million. After how many years will it be sold?
\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
9 & a & 1 & B & A34 & CN & \(05 / 76\) \\
& b & 4 & A & A34 & Ca & \\
\hline
\end{tabular}

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- \({ }^{1} \mathrm{pd}\) : evaluate at \(t=0\)
\(\bullet^{2}\) ic: substitute \(V=20\)
- \({ }^{3}\) pd: process
- \({ }^{4}\) ic: expo to \(\log\) conversion
- \({ }^{5}\) pd: solve a logarithmic equation

Primary Method : Give 1 mark for each •

- \({ }^{2} \quad 252 e^{-0.06335 t}=20\)
\(\bullet^{3} \quad e^{-0.06335 t}=\frac{20}{252}\)
-4 \(-0 \cdot 06335 t \log _{k}(e)=\log _{k}\left(\frac{20}{252}\right)\)
where \(k=e\) or \(k=10\)
-5 \(t=40 \quad\) [Note 1]

Alternative 2
- \(2 \quad 252 e^{-0.06335 t}=20\)
- \(\quad \log 252-0.06335 t \log e=\log 20\)
- \({ }^{4} \quad 5.53-0.06335 t=2.99\)
-5 \(\quad t=40\)

\section*{Alternative 3}
\[
\begin{array}{ll}
\bullet^{2} & 252 e^{-0.06335 t}=20 \\
\bullet^{3} & \ln 252+\ln e^{-0.06335 t}=\ln 20 \\
\bullet^{4} & -0.06335 t \ln e=\ln 20-\ln 252 \\
\bullet^{5} & t=40
\end{array}
\]

Note
You could also graph, for example, \(y=252 e^{-0.06335 t}\) and \(y=20\)

10
Vectors a and c are represented by two sides of an equilateral triangle with sides of length 3 units，as shown in the diagram． Vector b is 2 units long and b is perpendicular to both a and Evaluate the scalar product \(\boldsymbol{a} \cdot(\boldsymbol{a}+\boldsymbol{b}+\boldsymbol{c})\) ．



\section*{Notes}

1 Treat \(\underline{a}_{\text {＿}}\) ．\(⿴ 囗 十\) ritten as \(a^{2}\) as bad form．
2 Treat \(\underline{a}_{\text {＿}}\) ．britten as \(a b\) as an error unless it is subsequently evaluated as a scalar product．Similarly for \(\underline{a}_{\text {＿}}\) ，

3 Using \(\underline{\mathrm{p}}_{-} \mathrm{F}^{\boldsymbol{q}} p \| q \mid \sin \theta\) consistently loses 1 mark．（ie max． available is 3 ）

4 When attaching the components
\(\boldsymbol{c}=\left(\begin{array}{l}3 \\ 0 \\ 0\end{array}\right), \boldsymbol{b}=\left(\begin{array}{l}0 \\ 0 \\ 2\end{array}\right), \boldsymbol{a}=\left(\begin{array}{c}\frac{3}{2} \\ \frac{3 \sqrt{3}}{2} \\ 0\end{array}\right)\), all marks are available．
When attaching the components
\(\boldsymbol{c}=\left(\begin{array}{l}3 \\ 0 \\ 0\end{array}\right), \boldsymbol{b}=\left(\begin{array}{l}0 \\ 0 \\ 2\end{array}\right), \boldsymbol{a}=\left(\begin{array}{l}0 \\ 3 \\ 0\end{array}\right)\), only \(\cdot \mathbf{1}\) is available．

\section*{CAVE}
\(a .(a+b+c)=a . a+a . b+a . c\)
followed by
\(a \cdot a=9\)
earns \(\bullet 1\) and \(\bullet 2\) ．
but
\(a .(a+b+c)=a . a+a . b+a . c\)
followed by
\(\boldsymbol{a} \cdot \boldsymbol{a}=9, \boldsymbol{a} \cdot \boldsymbol{c}=9, \boldsymbol{a} \cdot \boldsymbol{b}=6\)
earns \(\bullet 1\) only．
11 (a) Show that \(x=-1\) is a solution of the cubic equation \(x^{3}+p x^{2}+p x+1=0\).
(b) Hence find the range of values of \(p\) for which all the roots of the cubic equation are real.
\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
11 & a & 1 & C & A21 & CN & \(05 / 54\) \\
& b & 7 & A & A22 & CN & \\
\hline
\end{tabular}

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- 1 pd: evaluate the function at \(x=-1\)
- \({ }^{2}\) ss: strategy for finding other factors
- ic: quadratic factor
- \({ }^{4}\) ss: strategy for real roots
- 5 ic: substitute
- \({ }^{6}\) pd: process
- \({ }^{7}\) ss: starts to solve inequation
- 8 ic: complete

\section*{Notes}

1 For alternative method 1, •2
- 2 (as is \(\cdot 3\) also) is for interpreting the result of a synthetic division.
Candidates must show some acknowledgement of the result of the synthetic division. Although a statement w.r.t. the zero is preferable, accept something as simple as "underlining" the zero.

2 Treat "= 0" missing at •3 as Bad Form
\(3 \cdot 4\) is only available as a consequence of obtaining a quadratic factor from a division of the cubic.

4 Using \(b^{2}-4 a c>0\) loses \(\cdot 4\)
An " \(\geq\) " must appear at least once somewhere between \(\cdot 4\) and \(\cdot 6\)

5 Where errors occur at the \(\cdot 3 / \cdot 5\) stages, then \(\cdot 6, \cdot 7, \cdot 8\) are still available for solving a ' 3 -term' quadratic inequation.

6 Evidence for •8 may be a table of values or a sketch

7 For candidates who start with \(\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}\), all marks are available (subject to working being equivalent to the Primary Method).

8 Wrong disciminant:
Using \(b^{2}+4 a c\) only \(\cdot 5\) (out of the last 5 marks) is available.
Any other expression masquerading as the discriminant loses all of the last 5 marks.
```

Primary Method : Give 1 mark for each •
- ${ }^{1} \quad f(-1)=-1+p-p+1=0 \quad 1$ mark

    \(\bullet-1\)\begin{tabular}{|llll|}
    \hline 1 \& $p$ \& $p$ \& 1 <br>
\& -1 \& $1-p$ \& -1 <br>
\hline 1 \& $p-1$ \& 1 \& 0
\end{tabular},$~$

    -3 \(x^{2}+(p-1) x+1=0 \quad\) [Note 2]
    -4 " \(b^{2}-4 a c\) " \(\mathrm{n} \quad \mathrm{n}\) (d)" [Notes 3,4]
    - \(5(p-1)^{2}-4\)
    - \({ }^{6} \quad(p-3)(p+1)\)
    - \({ }^{7} \quad p=3, p=-1\)
    \({ }^{8} \quad p \leq-1, p \geq 3\)
    [Note 6]
    7 marks
    ```

Alternative method 1 for marks 1,2 (starting with synth. division)
\(\begin{array}{rllll}\cdot^{1} & -1 & \begin{array}{llll}1 & p & p & 1 \\ & -1\end{array} & 1-p & -1 \\ & 1 & p-1 & 1 & 0\end{array}\)
\(\bullet^{2} \quad f(-1)=0\)
[Note 1]
etc

\section*{Marks should still be recorded as out of 1 and 7}

\section*{Alternative method 2 for marks 1,2 (quad. factor obtained by inspection)}
- \({ }^{1} \quad f(-1)=-1+p-p+1=0\)
- \({ }^{2} \quad f(x)=(x+1)\left(x^{2} \ldots \ldots \ldots\right)\)
etc

Common Error 1 (marks 5 to 8)
\((p-1)^{2}-4 \geq 0\)
\((p-1)^{2} \geq 4\)
\(p-1 \geq 2\)
\(p \geq 3\)
a \(\quad\) w a r d \(\quad 2 \quad m \quad a \quad r \quad k \quad s \quad o \quad u \quad t \quad o \quad f\)
[4] The scatter diagram shows 5 pairs of data values for \(x\) and \(y\) where \(\Sigma x=30, \Sigma y=26, \Sigma x^{2}=220, \Sigma y^{2}=168\) and \(\Sigma x y=120\).
(a) Find the equation of the regression line.
(b) Estimate the value of \(y\) when \(x=5\).

\begin{tabular}{|lllllll|}
\hline \hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
S1 & & 4 & C & 4.4 .2 & Ca & \(05 / 76\) \\
& b & 1 & C & 4.4 .2 & CN & \\
\hline
\end{tabular}

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- \(1 \quad \mathrm{pd}:\) calculate \(\mathrm{S}_{x y}\)
- \({ }^{2}\) pd: calculate \(\mathrm{S}_{x x}\)
- \({ }^{3}\) pd: calculate \(b\)
- \({ }^{4}\) pd: calculate \(a \&\) state equ.
- \({ }^{5}\) ic: use equ. of regression line

Primary Method : Give 1 mark for each •
- \({ }^{1} S_{x y}=-36\)
-2 \(S_{x x}=40\)
- \({ }^{3} \quad b=-0.9\)
\(\bullet^{4} \quad a=10 \cdot 6\) a \(\quad \mathrm{n} y=\operatorname{dll} 0 \cdot 6-0 \cdot 9 x \quad 4\) marks
- \(y_{x=5}=6.1\)

1 mark
[7] The diagram represents the probability density function for a continuous random variable \(X\).
(a) Find the value of \(k\).
(b) Find the median.

\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
S4 & a & 3 & A & 4.3 .1 & CN & \(05 / 83\) \\
& b & 2 & A & 4.3 .5 & CN & \\
\hline
\end{tabular}

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- \({ }^{1} \quad\) ss: \(\quad\) state total area \(=1\)
- \({ }^{2}\) ic: find expression for total area
- \({ }^{3}\) pd: process
- 4 ss: know total area \(=0.5\)
- \({ }^{5}\) pd: process

Primary Method : Give 1 mark for each \(\cdot\)
\[
\begin{array}{ll}
\bullet^{1} & \text { area }=1 \\
\bullet^{2} & 0 \cdot 1+0 \cdot 6+\frac{1}{2}(k-8) \times 0.1 \\
\bullet^{3} & k=14 \\
\bullet & 0 \cdot 1+(m-2) \times 0.1=\frac{1}{2}
\end{array}
\]
- \(5 \quad m=6\)

2 marks
[9] (a) Explain briefly the difference between sample standard deviation
(b) In statistics mode, a calculator shows the summary statistics for a certain data set.

One data value, \(1 \cdot 2\), is shown to be erroneous and is deleted.
Calculate the sample standard deviation of the new data set of 19 values correct to 3 decimal places.
\begin{tabular}{lr}
\(\bar{x}=\) & 2.325 \\
\(S_{x}=\) & 0.573883355 \\
\(\sigma_{x}=\) & 0.559352304 \\
\(\Sigma x=\) & 46.5 \\
\(\Sigma x^{2}=\) & 114.37 \\
\(n=\) & 20 \\
\(x_{\min }=\) & 1.2 \\
\(x_{\max }=\) & 3.2
\end{tabular} and range as measures of spread.
marks Grade Syllabus Code \(\begin{array}{ll}\text { 4.2.11/12 } & \text { CN } \\ 4.1 .1 & \text { Ca }\end{array}\)
\begin{tabular}{ll} 
Calculator class & \begin{tabular}{l} 
Source \\
CN
\end{tabular} \\
Ca & \(05 / 79\)
\end{tabular}

Primary Method : Give 1 mark for each -
- \({ }^{1}\) SD is a measure of spread about mean
whereas \(\left(x_{\max }-x_{\text {min }}\right)\) is a measure of range. 1 mark
- \({ }^{2} \quad \Sigma x=45.3\)
- \(\quad \Sigma x^{2}=112.93\)
- \({ }^{4} \quad S=\sqrt{\frac{1}{18}\left(112.93-\frac{45.3^{2}}{19}\right)}\)
- \(50 \cdot 523\)

4 marks
[10] A large organisation decides to run a mini-lottery for charity.
- Each participant selects any three different numbers from 1 to 20 inclusive.
- Every Friday the three winning numbers are drawn at random from the 20.
- Each participant with these winning numbers shares the jackpot.
(a) Find the number of possible combinations and hence find the probability of a particular combination winning a share of the jackpot.
(b) Find the probability that someone chooses the winning combination exactly twice within 3 successive weeks.
\begin{tabular}{|lllllll|}
\hline Qu. & part & marks & Grade & Syllabus Code & Calculator class & Source \\
S4 & a & 2 & B & \(4.2 .5,4.2 .3\) & Ca & \(05 / 78\) \\
& b & 3 & A & 4.2 .7 & Ca & \\
\hline
\end{tabular}

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- \({ }^{1}\) ss: find combination
- \({ }^{2}\) pd: calculate probability
- \({ }^{3}\) ic: interpret p (win)
- \({ }^{4}\) ss: find combination
- \({ }^{5}\) pd: process

Primary Method : Give 1 mark for each •
- \({ }^{1} \quad\) No. of outcomes \(=\binom{20}{3}\)
- 2 prob \(=\frac{1}{\binom{20}{3}}=\frac{1}{1140}\) 2 marks
-3 \(p(L)=\frac{1139}{1140}\)
- \(4 \quad p(2\) wins in 3\()\)
\(=3 \times\left(\frac{1}{1140}\right)^{2} \times\left(\frac{1139}{1140}\right)\)
- \(5 \quad 2.306 \times 10^{-6}\)```

